



# 15th Global Conference of Actuaries Plenary Session - Actuarial Frontiers

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## Modelling and Managing Longevity Risks

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# Coverage

- Global Pensions and Longevity Risk
- Longevity Risk Modelling and Management Frontiers
- Research projects in CEPAR and School of Risk and Actuarial Studies at UNSW
- Areas:
  - consistent framework for stochastic mortality
  - age-period-cohort models
  - longitudinal mortality risk factors and Norwegian mortality
  - modelling cause of death and cause elimination
  - regulation and capital requirements for life annuities in an insurer value maximisation framework
  - residential house price risk modelling and applications
  - health risk and financing long term care including reverse mortgages

# Pension Systems Asia Pacific

- Predominantly Public DB and DC schemes
- Private mandated DC schemes – Australia

[Pensions at a Glance Asia/Pacific 2011 - © OECD 2011](#)

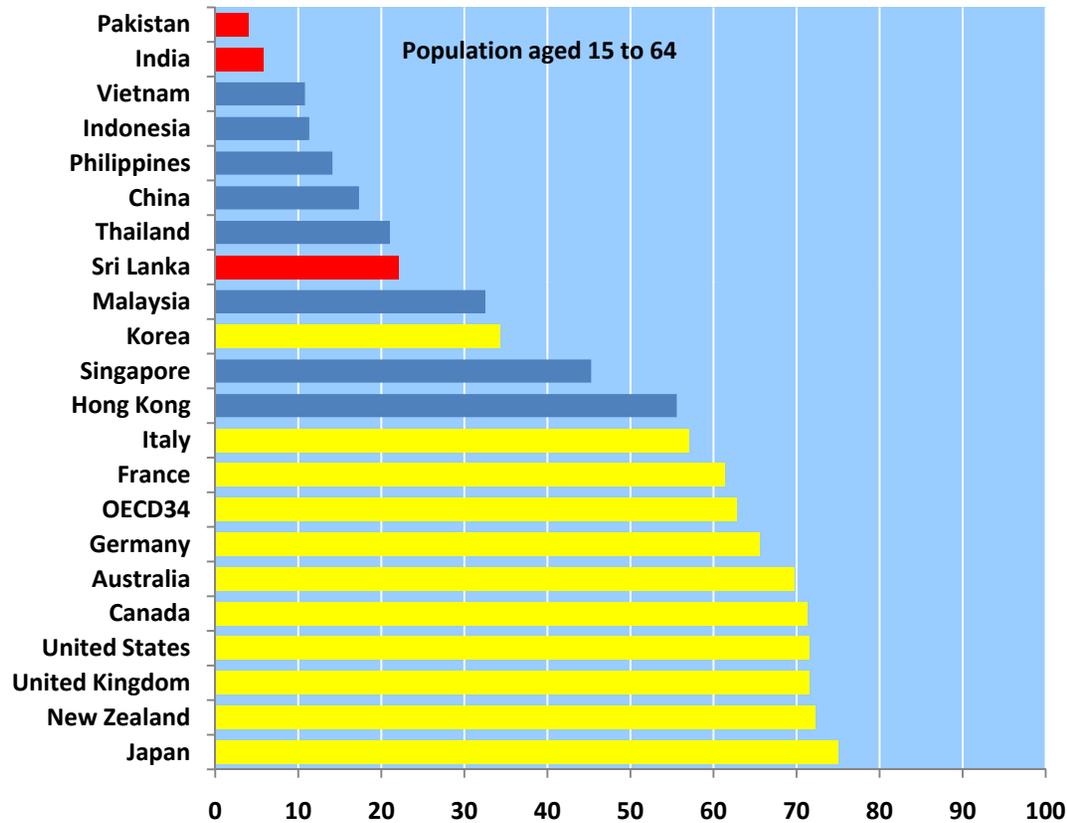
Executive Summary Table 1. Pensions in Asia/Pacific

Version 1 - Last updated: 30-Nov-2011

**Table 1. Pensions in Asia/Pacific**

Country	Type of pension scheme			Country	Type of pension scheme		
	Public		Private		Public		Private
	DB	DC	DC		DB	DC	DC
<b>East Asia/Pacific</b>				<b>South Asia</b>			
China		•		India	•	•	
Hong Kong, China			•	Pakistan	•		
Indonesia		•		Sri Lanka		•	
Malaysia		•		<b>OECD Asia/Pacific</b>			
Philippines	•			Australia			•
Singapore		•		Canada	•		
Thailand	•			Japan	•		
Vietnam	•			Korea	•		
				New Zealand			
				United States	•		

# Coverage of Mandatory Pension Schemes

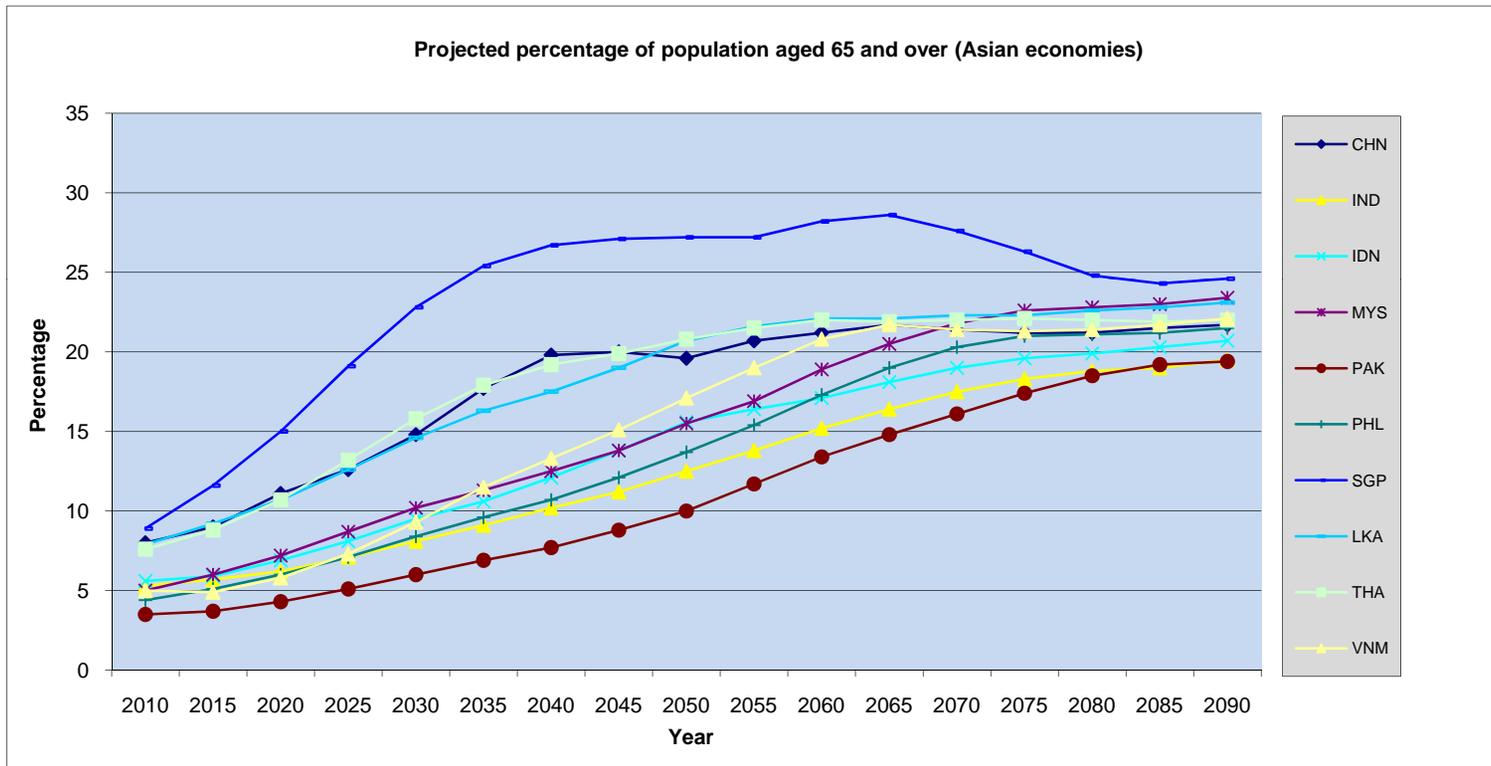


- Relatively low coverage in Asia/Pacific countries

- Potential future increases in coverage and funding implications

Source: PENSIONS AT A GLANCE ASIA/PACIFIC 2011 © OECD 2012 World Bank Pension Database

# Population Ageing - Asia



- Ageing across the region
- Implications for retirement and long term care and health costs

Source: PENSIONS AT A GLANCE ASIA/PACIFIC 2011 © OECD 2012

# Consistent Dynamic Mortality Model

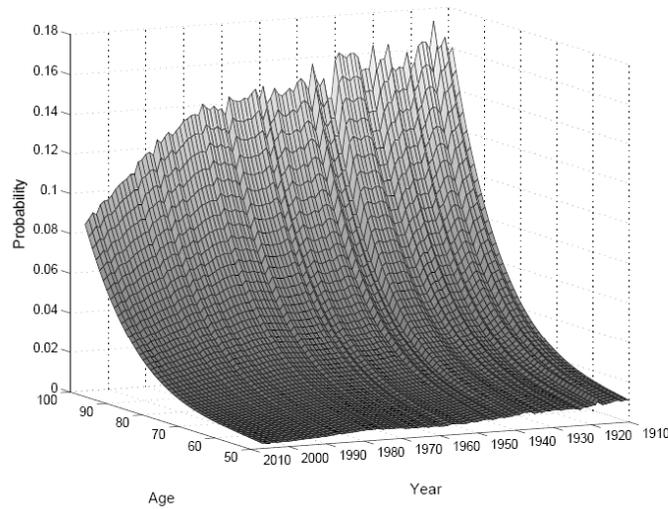
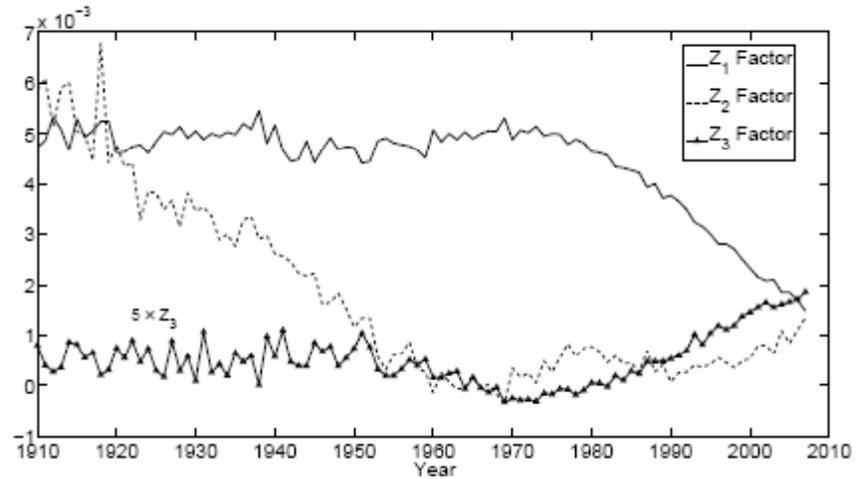


Figure 1: Population  $\bar{\mu}(t, T)$

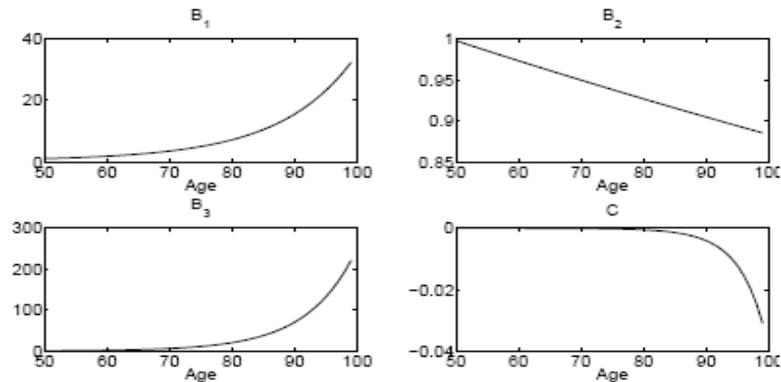


(a) Factors

Survivor curve

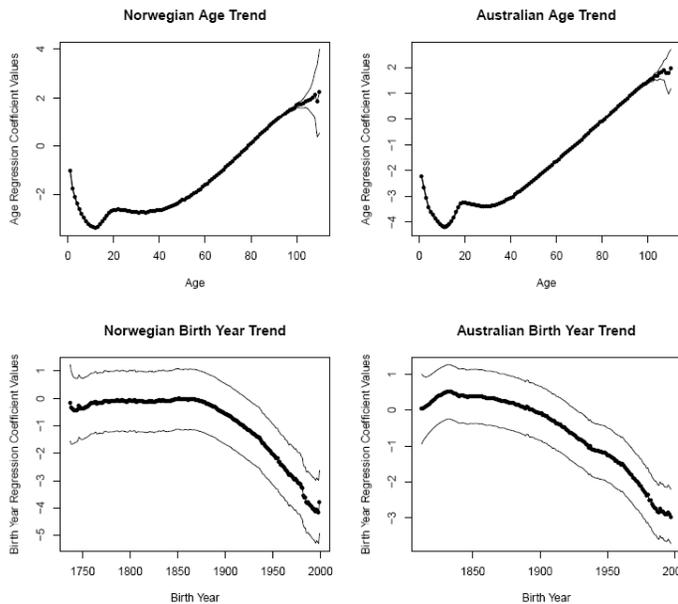
Multiple factors

Swedish mortality 1910 to 2007  
ages 50 to 100



(b) Factor Loadings

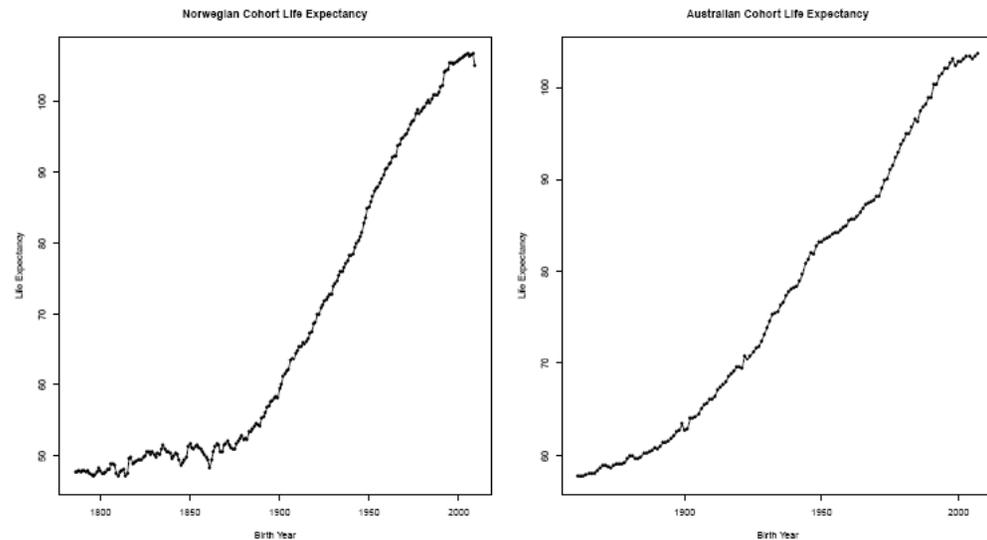
# Age – Period – Cohort Models



Trend models - birth year or cohort effect a significant trend factor

Period effects less significant (Spanish flu)

Links to Lee-Carter



# Longitudinal Analysis – HRS and Norwegian Data

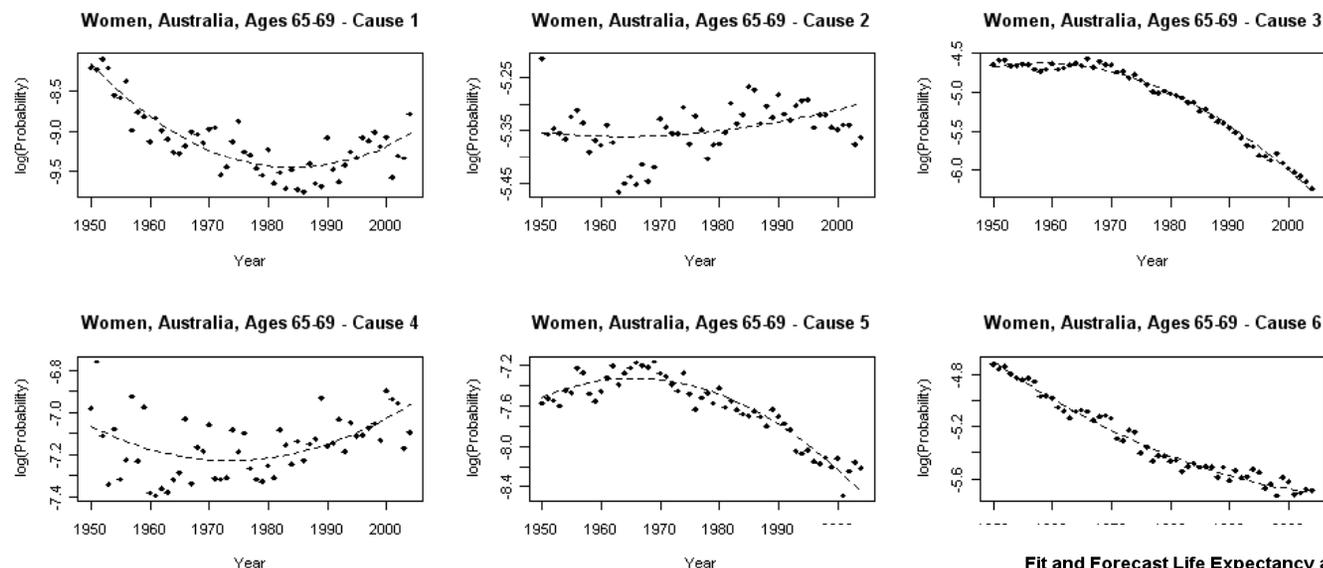
Panel data and logistic models

Mortality risk factors at an individual level

		Current Value Covariates			
		-2 LOG L		34,746	
		AIC		34,816	
		SBC		35,013	
		$\beta_k$	$h_k$	St.Dev	$\beta_k$
	Age	0.0571	1.0587	0.0072	***
	Male	0.4894	1.6314	0.0504	***
Education Ref: GED, HS or Some Coll.	<High School	-0.1536	0.8576	0.0510	***
	College +	0.0068	1.0068	0.0767	
Self-Report Health Ref: Good	Excellent	-0.6658	0.5139	0.1231	***
	Very Good	-0.3543	0.7017	0.0801	***
	Fair	0.5389	1.7141	0.0645	***
	Poor	1.1046	3.0181	0.0714	***
BMI Ref: Normal Weight	Underweight	0.8746	2.3979	0.1038	***
	Overweight	-0.3434	0.7094	0.0544	***
	Obese	-0.5474	0.5784	0.0697	***
	Morb. Obese	-0.4199	0.6571	0.0820	***
	Drinks Ever	-0.1214	0.8857	0.0491	**
	Smokes Ever	0.3693	1.4467	0.0592	***
	Smokes Now	0.2728	1.3136	0.0538	***
Health History	High BP	0.2425	1.2744	0.0499	***
	Diabetes	0.5452	1.7250	0.0515	***
	Cancer	0.7984	2.2219	0.0545	***
	Lung Disease	0.3922	1.4803	0.0574	***
	Heart Prob.	0.2906	1.3372	0.0504	***
	Stroke	0.3841	1.4684	0.0639	***
	Psych. Prob.	0.1200	1.1275	0.0588	**
	Arthritis	-0.1556	0.8559	0.0483	***

Table: Proportional hazards model.

# Causal Mortality Modelling

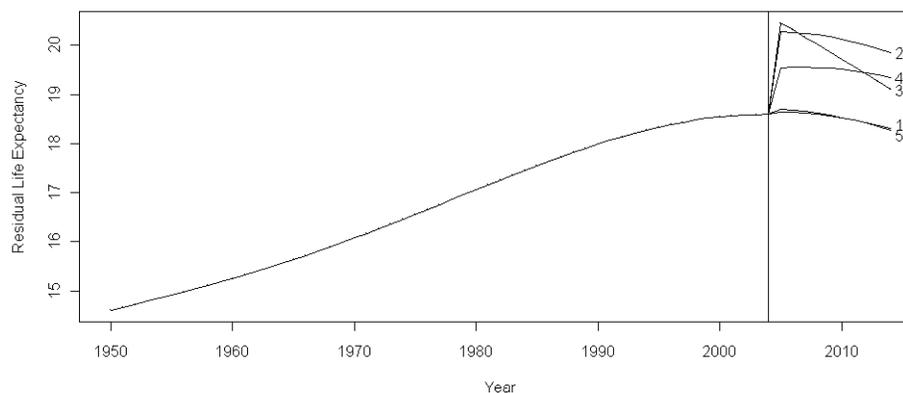


Simultaneously modelled periodic mortality trends by cause-of-death.

The impact on life expectancy under cause-elimination.

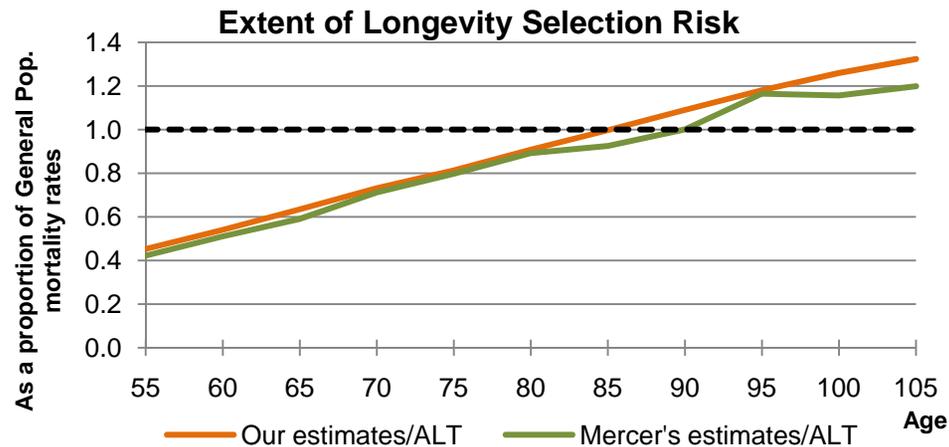
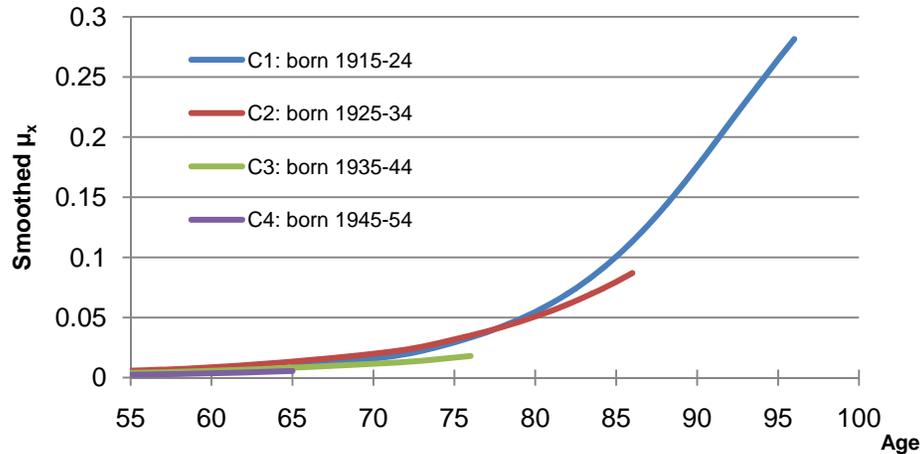
Inherent dependencies among *competing* causes is accounted for!

Fit and Forecast Life Expectancy at Age 65 for Women in Australia



# PwC-Mercer Pensioner Data

Pensioners by cohorts (Relevant ages)



Hazard Ratios (Cox PH model)

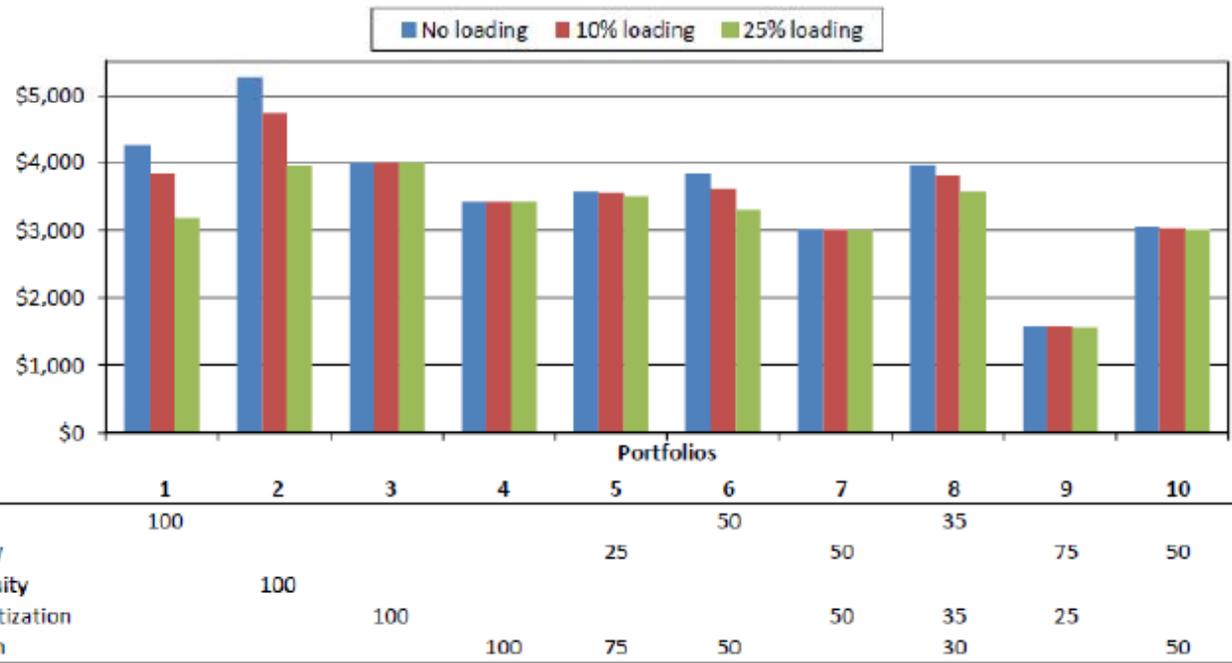
	Males	Females
<i>Pension sizes:</i>		
Low	1.23***	1.13***
Average (ref.)	1.00	1.00
High	0.64***	0.77***
<i>Specific schemes:</i>		
Federal-CSS (ref.)	1.00	1.00
Federal-PSS	0.71***	0.84
NSW-SSS	NA <sup>(b)</sup>	1.05
NSW-SASS	NA <sup>(b)</sup>	0.90
NSW-PSS	NA <sup>(b)</sup>	NA <sup>(a)</sup>
NSW-EISS	NA <sup>(b)</sup>	NA <sup>(a)</sup>
Victoria-SSS	NA <sup>(b)</sup>	NA <sup>(b)</sup>
Victoria-ESSS	1.01	0.86
South Aust-SASS	NA <sup>(b)</sup>	NA <sup>(b)</sup>
Tasmania-RBF	1.00	1.01
Western Aust-GESB	1.07**	1.16**
Queensland-SS	NA <sup>(b)</sup>	0.97
Queensland-PS	1.38	NA <sup>(a)</sup>
Grouped schemes	1.03**	1.13***
# subjects	111,257	47,350
Chi-squared	1,162	102
df	8	10
Adjusted R2	3.2%	1.1%

# Retirement Income Product Portfolios

Importance of GSA (mutual risk sharing) when guarantee products include loadings (capital costs)

Indexed annuities dominate

Phased withdrawals (bequest motive) and deferred annuity

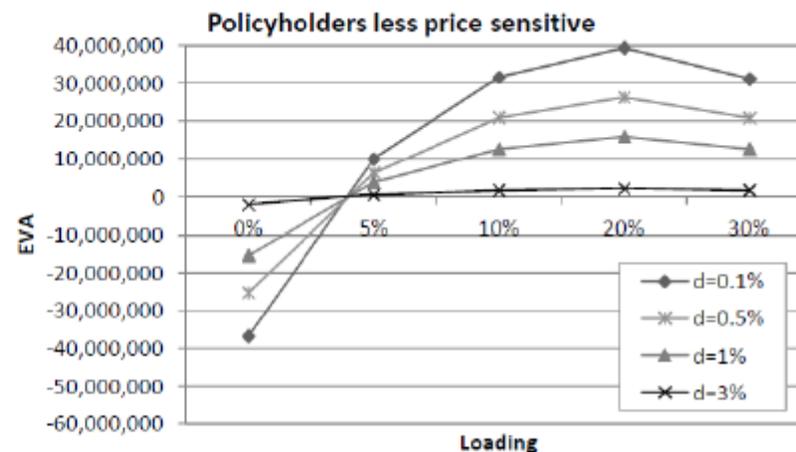
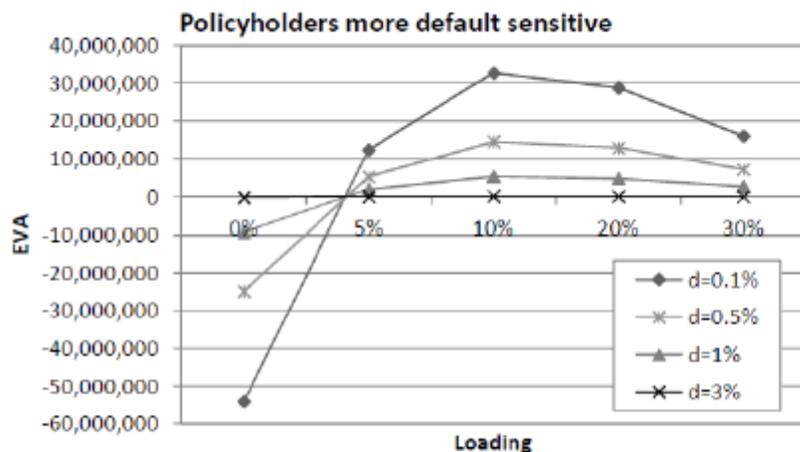
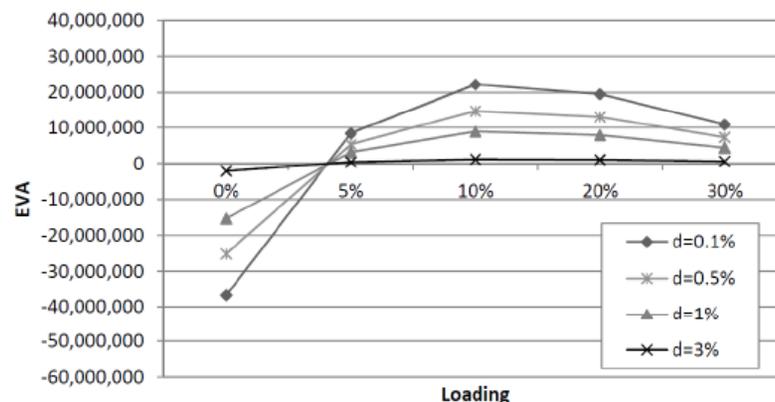


Hanewald, Piggott and Sherris (2011), Individual Post-Retirement Longevity Risk Management Under Systematic Mortality Risk.

# Solvency and Pricing for Life Annuities

Different default levels: optimal loading that maximises EVA

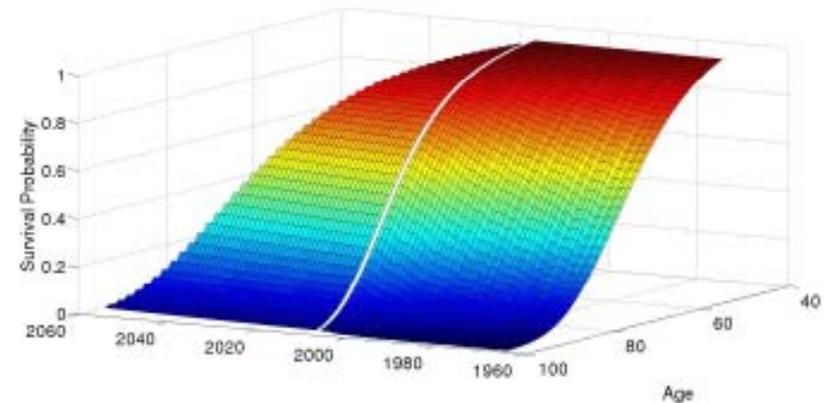
Sensitivity to solvency has important impact on value



# Life Insurer Longevity Risk Management

A multi-period stochastic model for an annuity provider facing systematic and idiosyncratic longevity risk

- Capital, premium loading, longevity swap, longevity bond
- Frictional costs vs. costs for transferring longevity risk



*Survival curve forecast based on Affine Term Structure Model in Blackburn and Sherris (2012)*

Variable	Longevity Swap	Longevity Bond
Benefits:	$b \cdot \tilde{N}(t; x)$	$b \cdot \tilde{N}(t; x)^{[\text{syst}]}$
Premium:	$b \cdot (1 + \lambda^{[\text{LS}]}) \cdot N_0(t; x)$	$b \cdot (1 + \lambda^{[\text{LB}]}) \cdot \mathbb{E}_0[\tilde{N}(t; x)]$

**Thank you**

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# Australian Research Council Linkage Grant

## **ARC Linkage Project 2008 LP0883398**

### **Managing Risk with Insurance and Superannuation as Individuals Age (2009-2013)**

**Industry Partners: PwC, APRA, World Bank**

- **Longevity Risk Models**
  - Models to quantify risks related to longevity and morbidity
- **Product Risk Management and Residential Housing**
  - Pricing, solvency, risk management and regulatory requirements for the prudential operation of longevity markets and institutions
- **Policy and Regulation**
  - Prudential and policy implications of new product innovations in both retail and wholesale financial markets

# ARC Centre of Excellence in Population Ageing Research (CEPAR)

<http://www.cepar.edu.au/>

**Collaborating universities: UNSW, The University of Sydney and the Australian National University (ANU)**

- *The ARC Centre of Excellence in Population Ageing Research brings together researchers, government and industry to address one of the major social challenges of the twenty first century. It will establish Australia as a world leader in the field of population ageing research through a unique combination of high level, cross-disciplinary expertise drawn from Economics, Psychology, Sociology, Epidemiology, Actuarial Science, and Demography.*

## For information:

# ARC Longevity Linkage Project Research Working Papers

### 2009 and 2010

- S. Wills and M. Sherris: Integrating Financial and Demographic Longevity Risk Models ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1139724](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1139724))
- S. Wills and M. Sherris: Securitization, Structuring and Pricing of Longevity Risk ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1139726](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1139726))
- Y. Choi and C. Kim: Securitization of Longevity Risks using Percentile Tranche Methods ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1349398](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1349398))
- C. N. Njenga and M. Sherris: Longevity Risk and the Econometric Analysis of Mortality Trends and Volatility ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1458084](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1458084))
- A. Ngai and M. Sherris: Longevity Risk Management for Life and Variable Annuities ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1587890](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1587890))
- J. Evans and M. Sherris: Longevity Risk Management and the Development of a Life Annuity Market in Australia ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1585563](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1585563))
- D. Sun and M. Sherris: Risk Based Capital and Pricing for Reverse Mortgages Revisited ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1588342](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1588342))
- A. Tang and M. Sherris: Spatial Variability in Mortality and Socioeconomic Factors for Australian Mortality ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1594522](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1594522))
- S. Gaille and M. Sherris: Age Patterns and Trends in Mortality by Cause of Death and Implications for Modeling Longevity Risk ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1694272](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1694272))
- S. Gaille and M. Sherris: Modeling Long-Run Cause of Death Mortality Trends ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1705696](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1705696))
- S. Gaille and M. Sherris: Improving Longevity and Mortality Risk Models with Common Stochastic Long-Run Trends ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1702029](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1702029))
- J. R. Piggott and H. Bateman: Too Much Risk to Insure? The Australian (Non-) Market for Annuities ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1706900](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1706900))
- C. S. Kumru and J. R. Piggott: Should Public retirement Provision be Means-tested? ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1417763](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1417763))
- R. Sane and J. R. Piggott: Elderly mobility and Trade-downs in Australia

## For information:

# ARC Longevity Linkage Project Research Working Papers

### 2011

- M. Sherris and S. Su: Heterogeneity of Australian Population Mortality and Implications for a Viable Life Annuity Market ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1779442](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1779442))
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- D.H. Alai and M. Sherris: Rethinking Age-Period-Cohort Mortality Trend Models ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1838805](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1838805))
- K. Hanewald, J. R. Piggott, and Michael Sherris: Individual Post-Retirement Longevity Risk Management Under Systematic Mortality Risk ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1910961](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1910961))
- K. Hanewald and M. Sherris: House Price Risk Models for Banking and Insurance Applications ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1961402](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1961402))
- D. P. Blake, C. Courbage, R. D. MacMinn and M. Sherris: Longevity Risks and Capital Markets: The 2010-2011 Update ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1964636](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1964636))

## For information:

# ARC Longevity Linkage Project Research Working Papers

### 2012

- J. Ziveyi, C. Blackburn, and M. Sherris: Pricing European Options on Deferred Insurance Contracts ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2005461](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2005461))
- H. Chen , M. Sherris , T. Sun and W. Zhu: Living with Ambiguity: Pricing Mortality-Linked Securities with Smooth Ambiguity Preferences ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2007342](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2007342))
- M. Sherris and D. TP Ho Quang: Portfolio Selection for Insurance Linked Securities: An Application of Multiple Criteria Decision Making ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2020712](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2020712))
- M. Sherris and E. Veprauskaite: An Analysis of Reinsurance Optimisation in Life Insurance ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2029314](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2029314))
- D. H. Alai , Z. Landsman and M. Sherris: Lifetime Dependence Modelling Using the Truncated Multivariate Gamma Distribution ([http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2033454](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=2033454))
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